CONTROL OF FLOW OVER A BLUFF BODY

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ABSTRACT
In this paper, we present our recent research activities on control of flow over a bluff body such as a circular cylinder, a two-dimensional bluff body with a blunt trailing edge and a sphere. First, we introduce a three-dimensional forcing applied to a two-dimensional bluff body and show that it significantly changes vortical structures in the wake and reduces mean drag and lift fluctuations. Second, by providing an appropriate active or passive control to a separating shear layer, one can destabilize the shear layer and reattach the flow on the surface before main separation, which delays main separation and decreases drag. Finally, we apply three different active control methods based on control theory (i.e., linear proportional feedback control, suboptimal feedback control, and active open-loop control using surrogate management framework) to flow over a sphere and show that they successfully reduce the lift fluctuations.

INTRODUCTION
The flow over a bluff body is a common occurrence associated with fluid flowing over an obstacle or with the movement of a natural or an artificial body. Evident examples are the flows past an airplane, a submarine and an automobile, and wind blowing past a bridge and a high-rise building. At much low Reynolds numbers, the flow over a bluff body is highly viscous and the force exerted on the body is mainly attributed to the skin friction. However, when the Reynolds number exceeds a critical value, vortex shedding occurs in the wake, resulting in a significant pressure drop on the rear surface of the body. This vortex shedding occurs over a wide range of Reynolds numbers, causing serious structural vibrations, acoustic noise and resonance, enhanced mixing, and significant increases in the mean drag and the lift fluctuations. Therefore, the effective control of vortex shedding is important in engineering applications.

Efforts have been made to alter and suppress vortex shedding (see the reviews by Zdravkovich (1981), Oertel (1990), Griffin & Hall (1991) and Choi et al. (2008) for these research activities). In the past, many passive and active open-loop control methods were introduced to control vortex shedding behind a two-dimensional bluff body such as a circular cylinder and a two-dimensional blunt-based bluff body. Examples are the endplate, splitter plate, geometric modification in the trailing edge, base bleed, oscillation in line with the incident flow, and rotary oscillation. These control methods are passive or active open-loop in the sense that there is no power input or no feedback sensor, respectively.

Many attempts have been also made to improve the control efficiency and effectiveness using active feedback control methods with the advent of micro-electro-mechanical-system, development of control theory, and fast growth of computer power. The merit of this approach is to obtain the information of the response of flow system to the actuation, and to use it to obtain better control performance than that from the passive or active open-loop control method.

The purpose of this study is to develop effective methods for the control of flow over a bluff body. Three different control approaches are considered. First, we apply a three-dimensional forcing to a two-dimensional bluff body. Second, we provide an appropriate active or passive control to a separating shear layer for its destabilization. Third, we apply active control methods based on control theories (i.e., linear proportional feedback control, suboptimal feedback control, and active open-loop control using surrogate management framework) to flow over a sphere. For the shapes of bluff bodies, we consider a circular cylinder, a two-dimensional bluff body with a blunt trailing edge, and a sphere. The circular cylinder and sphere are the representative two- and three-dimensional bluff bodies, respectively, and their separation points change depending on the Reynolds number. On the other hand, in the case of two-dimensional blunt-based bluff body, the separation is fixed at the trailing edge and hence the flow suddenly changes at the trailing edge from a boundary-layer flow to wake, which is quite different from the cases of circular cylinder and sphere. Therefore, different control strategies may have to be developed when the body shapes are different. A part of the present paper is excerpted from a recent review paper of Choi et al. (2008).

THREE-DIMENSIONAL FORCING FOR TWO-DIMENSIONAL BLUFF BODY

In this section, we provide passive and active open-loop controls varying along the spanwise (or azimuthal) direction, called three-dimensional forcing, to control nominally two-dimensional wake.

Passive control
Examples of three-dimensional geometric modification are the helical strake, segmented trailing edge, wavy trailing edge on a blunt-based model, spanwise waviness to front stagnation face of a rectangular cylinder, circular cylinder with a sinusoidal axis, and circular cylinder with hemispherical bumps (see Choi et al. (2008) and references therein for more details).

We propose a small-size tab, mounted on a part of the upper and lower trailing edges of a two-dimensional bluff body (Fig. 1a; Park et al., 2006), for effectively attenuating vortex shedding and reducing drag. We perform a parametric study by varying the height (h) and width (l) of the tab and the spanwise spacing between the adjacent tabs (λ). Drag is decreased (or the base pressure is increased) by attaching this simple device at the trailing edge (see Fig.
the circular cylinder by Tokumaru & Dimotakis (1991) and reduce drag. One example is the high-frequency rotation of open-loop controls that attenuate vortex shedding and re-

and the lift fluctuations. There are a few successful active control methods employing the three-dimensional forcing in the literature. In Kim & Choi (2005), we numerically investigate the effect of the three-dimensional (called 'distributed') forcing on the drag and lift forces on a circular cylinder. The distributed forcing considered is a blowing and suction from the slots located at upper and lower surfaces of the cylinder. The blowing and suction profile from each slot is sinusoidal in the spanwise direction but is steady in time (Fig. 5a):

\[
\phi_1(z) = \phi_2(z) = \phi_0 \sin (2\pi z/\lambda),
\]

where \(\phi_1\) and \(\phi_2\) are the radial velocities at the upper and lower slots, respectively, \(z\) is the spanwise direction, \(\phi_0\) is the forcing amplitude, and \(\lambda\) is the forcing wavelength. For all

2). The optimal configuration of tabs produces about 33% increase in the base pressure. Owing to the tabs, the vortices shed from the upper and lower trailing edges lose their two-dimensional nature and the vortex dislocation occurs. The vortex shedding completely disappears right behind the bluff body but occurs weakly at farther downstream locations (Fig. 3). Since the main mechanism of drag reduction by the tab is to introduce the spanwise phase mismatch in the vortex shedding process and thus to break the nominally two-dimensional nature of vortex shedding, this passive device should work for other two-dimensional bluff bodies such as the circular cylinder.

Therefore, we apply this tab to flow over a circular cylinder at \(Re = 100\) (Fig. 1b). The tab located near the separation point reduces drag on a circular cylinder and attenuates the vortex shedding in the wake (Fig. 4). The optimal spanwise spacing between the adjacent tabs is similar to that in Darekar & Sherwin (2001).

However, for three-dimensional bluff bodies such as the sphere or some transportation vehicles, the vortical structures are essentially three dimensional (Yun et al., 2006). In this case, the three-dimensional geometric modifications described above may not produce any drag reduction because they promote three-dimensional vortical activities in the wake. Our preliminary study about flow over a three-dimensional body with the tab did not produce any drag reduction. Therefore, some other types of passive device should be developed for reduction of drag on a three-dimensional body.

Active open-loop control

When a time-periodic open-loop forcing is applied, vortex shedding in the wake is in general locked in phase to the forcing (Blevins, 1990), and consequently the forcing strengthens vortex shedding and increases the mean drag and the lift fluctuations. There are a few successful active open-loop controls that attenuate vortex shedding and reduce drag. One example is the high-frequency rotation of the circular cylinder by Tokumaru & Dimotakis (1991) and

![Figure 1: Three-dimensional forcing by tabs: (a) two-dimensional model vehicle; (b) circular cylinder.](image1)

![Figure 2: Contours of \(\Delta \bar{C}_{pb}\) with respect to \(\lambda\) and \(l_s\) at \(Re = 5000\): (a) \(l_s/h = 0.1\); (b) 0.133; (c) 0.2. \(\Delta \bar{C}_{pb}\) = \(\bar{C}_{pb}\) (controlled) - \(\bar{C}_{pb}\) (uncontrolled) \times 100, and \(\bar{C}_{pb}\) is the mean base-pressure coefficient. From Park et al. (2006).](image2)

![Figure 3: Contours of \(\Delta \bar{C}_{pb}\) with respect to \(\lambda\) and \(l_s\) at \(Re = 4000\): (a) \(l_s/h = 0.1\); (b) 0.133; (c) 0.2. \(\Delta \bar{C}_{pb}\) = \(\bar{C}_{pb}\) (controlled) - \(\bar{C}_{pb}\) (uncontrolled) \times 100, and \(\bar{C}_{pb}\) is the mean base-pressure coefficient. From Park et al. (2006).](image3)

another is the base bleed (Wood, 1964; Bearman, 1967). Although these controls are effective in reducing drag, their efficiencies are not so high.

There are only a few active control methods employing the three-dimensional forcing in the literature. In Kim & Choi (2005), we numerically investigate the effect of the three-dimensional forcing in the literature. In Kim & Choi (2005), we numerically investigate the effect of the three-dimensional forcing in the literature. In Kim & Choi (2005), we numerically investigate the effect of the three-dimensional forcing in the literature.
Figure 3: Instantaneous vortical structures in the wake ($Re = u_\infty h/\nu = 4,200$): (a) uncontrolled flow; (b) controlled flow with tabs of $(\lambda/h, l_y/h, l_z/h) = (2,0.2,0.2)$. Shown in this figure are the three-dimensional views of vortical structures (left column) and top views of iso-pressure surfaces (right column). From Park et al. (2006).

Figure 4: Flow over a circular cylinder with tabs of $(l_y/d, l_z/d) = (0.2,0.2)$ at $Re = u_\infty d/\nu = 100$: (a) variation of the drag coefficient with the spanwise spacing ($\lambda$) of tabs; (b) instantaneous vortical structures in the wake at $\lambda = 4d$. In (b), vortex shedding completely disappears due to the tab.

Figure 5: Distributed forcing by Kim & Choi (2005): (a) schematic of the forcing; (b) $Re = 100 (\lambda = 5d)$; (c) $Re = 3900 (\lambda = \pi d)$. Shown in (b) and (c) are the instantaneous vortical structures without (left column) and with (right column) control.

Figure 6: Spanwise variation of the separation angle due to the distributed forcing at $Re=100 (\lambda = 5d)$. From Kim & Choi (2005).

It is important to note that drag reduction by the distributed forcing is caused by the direct interaction with the Reynolds numbers larger than 46, the distributed forcing attenuates or annihilates the vortex shedding as shown in Figs. 5(b) and (c), and thus significantly reduces the mean drag and the drag and lift fluctuations. Note that, due to the control, vortex shedding completely disappears at $Re = 100$ (Fig. 5b), and nearly disappears in the near wake and reappears weakly in the far wake at $Re = 3900$ (Fig. 5c). The distributed forcing produces the phase mismatch along the spanwise direction in vortex shedding, weakens the strength of vortical structures in the wake, and thus reduces drag.

vortex shedding, not by the separation delay: as shown in Fig. 6, the separation angle delays at the suction locations but significantly advances at the blowing locations. This fact suggests that the distributed forcing should be also applicable to a body with fixed separation for drag reduction or reduction of lift fluctuations. Thus, we apply the distributed forcing to turbulent flow over a two-dimensional model vehicle having a blunt trailing edge and obtain a significant amount of drag reduction (Kim et al., 2004).

Therefore, the three-dimensional forcing should be applicable to flow over any two-dimensional bluff body, which contains nominally two-dimensional vortex shedding, for drag reduction at various Reynolds numbers.

**EARLY SEPARATION AND REATTACHMENT BEFORE**
In this section, we consider a sphere which has a movable separation point. For this shape, delay of main separation produces significant drag reduction. To achieve the separation delay, near-wall streamwise momentum should be enhanced near and before the separation point such that it can overcome the adverse pressure gradient formed in the rear part of bluff body. The enhancement of near-wall momentum can be realized by controls either through direct boundary layer transition to turbulence or through early separation and reattachment before main separation. In this study, we show some results from the latter approach.

In the uncontrolled flows over a circular cylinder and a sphere, the drag coefficients rapidly decrease down to about 0.25 and 0.07, respectively, and this phenomenon has been called as the drag crisis (Fage, 1936; Bearman, 1969; Achenbach, 1972; Farell & Blessmann, 1983). The cause of this rapid drag-coefficient reduction is known to be the existence of small separation bubble(s) above the surface (Fig. 7; Suryanarayana & Prabhu, 2000). At the critical Reynolds number, disturbances existing in the boundary layer rapidly grow along the separating shear layer and high momentum fluids in the free-stream are entrained toward the bluff-body surface. This causes the reattachment of the flow (thus forming a separation bubble above the surface) and generates strong near-wall momentum, resulting in the delay of main separation.

We conduct an active control of flow over a sphere for drag reduction using a local time-periodic blowing and suction at subcritical Reynolds numbers, $Re = 6 \times 10^4 \sim 2 \times 10^5$.
We also investigate the effect of free-stream turbulence on flow over a sphere by installing various types of grids upstream of the sphere. The free-stream turbulence generates small separation bubble above the sphere surface and decreases the critical Reynolds number at which the drag coefficient rapidly decreases (Fig. 12). With further increasing the Reynolds number, the laminar separation point is delayed downstream but the reattachment point closing the separation bubble is fixed at 115°. The main separation point is also fixed at around 130°, resulting in constant drag coefficient after the critical Reynolds number. As the Reynolds number is further increased, the small separation bubble finally disappears but the main separation point is still fixed at 130°. Therefore, the formation, regression and disappearance of the separation bubble are the key to the drag change due to the free-stream turbulence.

The drag on a sphere is also changed by a trip wire located at the same dimple irrespective of the Reynolds number. Three different trip-wire sizes are tested. (Fig. 11). Again, this mechanism is not very different from that of the drag crisis.

We apply a linear proportional control similar to that proposed by Park et al. (1994). The velocity at the centerline in the wake region is measured for feedback and the control input (blowing/suction) at a part of the sphere sur-
Figure 15: Time histories of the drag and lift coefficients and phase diagram (Re = 425): (a) time histories of drag coefficient; (b) time histories of the lift coefficient. Shown here is the case of $x_s = 1.2d$ and $\alpha = -0.5$.

![Figure 15: Time histories of the drag and lift coefficients and phase diagram (Re = 425): (a) time histories of drag coefficient; (b) time histories of the lift coefficient. Shown here is the case of $x_s = 1.2d$ and $\alpha = -0.5$.](image)

The face is determined by the measured velocity as follows (Fig. 14):

$$\psi(\theta) = \alpha |u_{r,sensed}| \cos(\theta - \theta')$$  \hspace{1cm} (2)

Here, $\psi$ is the wall-normal actuation velocity (blowing/suction), $\theta$ is the azimuthal angle, $\alpha$ is the feedback gain, $u_{r,sensed}$ is the measured radial velocity at the sensing position, $x_s$, and $\theta'$ is the azimuthal angle of measured velocity. Thus, the blowing/suction varies along the azimuthal direction and maximum blowing and suction occur in phase and out of phase to the measured velocity at $x_s$. Also the amplitude of blowing/suction linearly increases as the measured velocity increases. For the actuation location, we set $\phi = 100^\circ$ and $\Delta \phi = 20^\circ$ (see Fig. 14).

We consider $Re = 425$, at which the base flow is unsteady asymmetric. Among various $x_s$’s and $\alpha$’s tested, the most effective sensing position and amplitude are $x_s = 1.2d$ and $\alpha = -0.5$, respectively. Figure 15 shows the time histories of drag and lift coefficients. Here, the lift coefficient is defined as $C_L = \sqrt{C_y^2 + C_z^2}$. The drag and lift fluctuations are significantly reduced by the control. However, the mean drag is almost unchanged.

The present control method strongly depends on the feedback gain $\alpha$ and sensing position $x_s$. As shown in Fig. 16, when the sensing position or the feedback gain is changed slightly, the drag increases significantly. The fluctuations of lift coefficient are closely related with vortex shedding, and thus it is important to know the sensor location at which the radial velocity along the centerline in the wake is connected with vortex shedding. For this purpose, we define a correlation function as follows:

$$C(x) = \frac{1}{T} \int_0^T \cos(\theta_{CL} - \theta_{ur}) dt,$$  \hspace{1cm} (3)

where $\theta_{CL}$ is the azimuthal angle of lift direction, $\theta_{ur}$ is the azimuthal angle of the direction of measured velocity at the sensing location, and $T$ is the time period of averaging. The value of $C(x)$ becomes 1 when the directions of lift and measured velocity are equal from each other, and -1 when the directions are opposite. Thus, when $|C(x)| \rightarrow 1$, the lift force and measured velocity are well correlated. Figure 17 shows the variation of $C(x)$ with $x_s$. A strong negative correlation occurs at $x_s = 1.2d$. This location is in good agreement with the $x_s$ location where the control performs well.

![Figure 16: Variations of the drag coefficient with the sensing position and feedback gain (Re = 425): (a) – – –, $x_s/d = 1.1$; ----, 1.2; -.-.-, 1.3 ($\alpha = -0.5$); (b) – – –, $\alpha = -0.4$; ----, -0.5; -.-.-, -0.6 ($x_s/d = 1.2$).](image)

![Figure 17: Correlation of the azimuthal angles between the lift and measured velocity (Re = 425).](image)
the control input was determined based on the measurement of instantaneous surface pressure. As a result, vortex shedding became weak or disappeared, and the mean drag and drag/lift fluctuations significantly decreased.

We also apply a suboptimal control to flow over a sphere at \( Re = 425 \). The cost function to be minimized is the difference between the real and potential pressures on the sphere surface (Fig. 18a). The control input is the blowing and suction on the sphere surface and is determined from the measurement of instantaneous surface pressure (Fig. 18b). As a result, we obtain a significant drag reduction through the change in the vortical structures (Figs. 18c and d).

**Surrogate Management Framework (SMF)**

In the present study, we apply SMF to flow over a sphere to reduce the drag. In the previous sub-section, we applied suboptimal control to the flow over a sphere. As shown in Fig. 18(b), the blowing/suction profile has a wavy shape. Therefore, we adopt sinusoidal blowing/suction as a base function for SMF. The blowing/suction velocity is given as follows:

\[
\psi(\phi) = \alpha \left( \psi_{10}(\phi) - \bar{\psi} \right),
\]

\[
\alpha^2 = \frac{0.01}{\int \int (\psi_{10}(\phi) - \bar{\psi})^2 r^2 \sin \phi \sin d\phi d\theta},
\]

\[
\psi_{10}(\phi) = A \cos 2\phi - B \sin 2\phi,
\]

\[
\bar{\psi} = \frac{1}{\pi} \int \int (A \cos 2\phi - B \sin 2\phi) r^2 \sin \phi \sin d\phi d\theta.
\]

Here, \( r \) is the radial direction, \( 0 \leq \phi < 180^\circ \), \( \theta \) is the azimuthal direction (\( 0 \leq \theta < 360^\circ \)). The parameters \( A \) and \( B \) are determined through SMF, with the constraints of \(-1 < A < 1 \) and \(-1 < B < 1 \). The blowing/suction velocity is homogeneous in the azimuthal direction.

Figure 19 shows the optimal blowing/suction profile obtained from SMF \((A = 0.5, B = -0.3)\), which produces about 17% drag reduction. Suction locates at \( 70^\circ < \phi < 140^\circ \), and blowing does elsewhere. Figure 20 shows vortical structures without and with control. As shown, the base flow (unsteady planar-symmetric structure) changes to be steady planar-symmetric with the control.

**Conclusions**

In this study, we presented three control methods applied to bluff-body flows. First, we introduced a three-dimensional forcing applied to a two-dimensional bluff body and showed that it significantly changes vortical structures in the wake and reduces mean drag and lift fluctuations. The control directly interacted with flow in the wake rather than through the change in the boundary layer before main separation. Therefore, this control can be applied to flows over two-dimensional bluff bodies with and without fixed separation. Second, by providing an appropriate active or passive control to a separating shear layer, we destabilized the shear layer and reattached the flow on the surface before main separation, which delayed main separation and decreased drag. This phenomenon is quite similar to what happens at the critical Reynolds number without any control. Finally, we applied active control methods based on control theories (i.e., linear proportional feedback control, suboptimal feedback control, and active open-loop control using surrogate management framework) to flow over a sphere. Three controls were all successful in reducing the lift fluctuations.
Figure 19: Optimal blowing/suction velocity from SMF.

Figure 20: Vortical structures at $Re = 300$: (a) without control; (b) with SMF control.

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